

A correction on the paper “A Note on Bi-Periodic Leonardo Sequence”

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The generating function in Theorem 3 of our work [1] was computed incorrectly. Below we provide the new version of Theorem 3 including the corrections to be made in its proof. The authors are grateful to Carlos M. Da Fonseca [2] for identifying this error.

The corrected version of Theorem 3 in [1] is as follows.

Theorem 3 *The generating function for bi-periodic Leonardo numbers is given by*

$$\sum_{n=0}^{\infty} GLe_n x^n = \frac{(2a - 1) + 2a(b - 1)x + (2 - a(b + 2))x^2 + 2ax^3 - x^4}{(1 - x)(1 - (ab + 2)x^2 + x^4)}. \quad (20)$$

The expression on line 4 page 9 in [1] should be read as

$$(1 - (ab + 2)x^2 + x^4)g(x) = (2ab - 1)x + (ab + 1)x^3 + ab \sum_{m=2}^{\infty} x^{2m+1}.$$

Then for

$$F(x) = \sum_{n=0}^{\infty} GLe_n x^n = h(x) + g(x),$$

we obtain

$$\begin{aligned} (1 - (ab + 2)x^2 + x^4)F(x) &= \\ &= (2a - 1) + (2ab - 1)x + (-2a + ab + 1)x^2 + (ab + 1)x^3 + ab \sum_{n=4}^{\infty} x^n = \\ &= (2a - 1) + (2ab - 1)x + (-2a + ab + 1)x^2 + (ab + 1)x^3 + \\ &\quad + ab \left(\frac{1}{1 - x} - 1 - x - x^2 - x^3 \right) \\ &= \frac{(2a - 1) + 2a(b - 1)x + (2 - a(b + 2))x^2 + 2ax^3 - x^4}{1 - x}. \end{aligned}$$

References

- [1] P.M.M. Catarino and E.V.P. Spreafico, A note on bi-periodic Leonardo sequence. *Armen. J. Math.*, 16 (2024), no. 5, pp. 1–17.
<https://doi.org/10.52737/18291163-2024.16.5-1-17>
- [2] C.M. da Fonseca, The generating function of a bi-periodic Leonardo sequence. *Armen. J. Math.*, 16 (2024), no. 7, pp. 1–8.
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